

## ON THE EFFECT OF CAVITATION ON THE RADIAL FORCES AND HYDRODYNAMIC

## STIFFNESS OF A CENTRIFUGAL PUMP\*

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The asymmetric flow within a volute exerts a radial force on a centrifugal impeller. The present paper presents experimental measurements of the radial forces on the impeller in the presence of cavitation.

## NOMENCLATURE

- [A] hydrodynamic force matrix, non-dimensionalized by  $\rho\omega^2 r_2^2 b_2$
- $A_1, A_2$  impeller inlet area ( $\pi r_1^2$ ), outlet area ( $2\pi r_2 b_2$ )
- $b_2$  impeller discharge width (0.62 in)
- {F} 6-component generalized force vector
- $F_1, F_2$  components of the instantaneous lateral force on the impeller in the rotating dynamometer reference frame
- $F_x, F_y$  components of the instantaneous lateral force on the impeller in the fixed laboratory reference frame (X,Y), non-dimensionalized by  $\rho\omega^2 r_2^3 b_2$
- $F_{ox}, F_{oy}$  values of  $F_x$  and  $F_y$  if the impeller was located at the the origin of the (X,Y) coordinate system (volute center), non-dimensionalized by  $\rho\omega^2 r_2^3 b_2$

\* The authors are indebted to the NASA George Marshall Space Flight Center, Alabama for continued sponsorship of this research under contract NAS8-33108. We are also grateful for the help given by D. Brennen.

$F_N, F_T$	components of the lateral force on the impeller normal to and tangential to the whirl orbit, averaged over the orbit, non-dimensionalized by $\rho\pi\omega^2 r_2^2 b_2 \epsilon$
	$F_N = (A_{xx} + A_{yy})/2 \quad F_T = (-A_{xy} + A_{yx})/2$
$p_1, p_{t1}$	upstream static, total pressure
$p_2, p_{t2}$	downstream static, total pressure
$p_I$	static pressure at impeller inlet, $p_{t1} - \rho(\frac{Q}{A_1})^2/2$
$p_v$	vapor pressure of water
$Q$	flow rate
$r_1, r_2$	impeller inlet, discharge radius (1.594 in., 3.188 in.)
$t$	time
$(X, Y)$	fixed laboratory reference frame
$x, y$	instantaneous coordinates of the impeller center in the fixed laboratory reference frame $(X, Y)$ , non-dimensionalized by $r_2$
$\epsilon$	radius of the circular whirl orbit
$\theta$	angle of the impeller on the eccentric circle, measured from the volute tongue in the direction of impeller rotation
$\rho$	density of water
$\sigma$	cavitation number, $\frac{p_I - p_v}{\rho\omega^2 r_1^2/2}$

- $\phi$  flow coefficient based on the impeller discharge area and tip speed,  $\frac{Q}{\omega r_2 A_2}$
- $\Phi$  total head coefficient,  $\frac{P_{t2} - P_{t1}}{\rho \omega^2 r_2^2}$
- $\omega$  radian frequency of the impeller (shaft) rotation

## INTRODUCTION

Earlier papers (refs.1-8) have described measurements of the radial forces and hydrodynamically induced rotordynamic coefficients of centrifugal pumps with various impellers and volutes. All of these earlier measurements were made in the absence of any cavitation within the pump. Yet there is some evidence that the presence of cavitation may have a significant effect on these forces and coefficients. Indeed some tests of the high speed pumps in the Space Shuttle Main Engine have suggested a change in the rotordynamics when cavitation occurs (ref. 9). The present paper is a supplement to our earlier measurements of forces and coefficients and constitutes an exploration of the influence of cavitation.

The references 6-8 provide a complete description of the facility. Briefly, the dynamometer, composed of two parallel plates connected by four strain gaged posts, is mounted between the impeller and the drive shaft. It measures the six components of a generalized hydrodynamic force vector  $\{F\}$  acting on the impeller. The impeller can be subject to whirling motion in an orbit eccentric to the volute center, in addition to the normal impeller rotation. Since the eccentric motion is in the lateral plane, perpendicular to the impeller centerline, only the two components of the force vector  $\{F\}$  in this lateral plane will be discussed.

These forces can be represented by

$$\begin{Bmatrix} F_x \\ F_y \end{Bmatrix} = \begin{Bmatrix} F_{ox} \\ F_{oy} \end{Bmatrix} + [A] \begin{Bmatrix} x \\ y \end{Bmatrix} \quad (1)$$

Referring to figure 1,  $F_x$  and  $F_y$  are in the volute frame of reference, and  $x$  and  $y$  represent the coordinates of the impeller center measured from the volute center. Dimensionless quantities are used throughout (see Nomenclature for definitions). The present results are only for the case of no whirl:  $x$  and  $y$  are fixed in time. When the impeller is located at an angular position,  $\theta$ , on the circular whirl orbit of radius  $\epsilon$ , equation (1) is written as

$$\begin{Bmatrix} F_x \\ F_y \end{Bmatrix} = \begin{Bmatrix} F_{ox} \\ F_{oy} \end{Bmatrix} + [A] \begin{Bmatrix} \epsilon/r_2 \cos\theta \\ \epsilon/r_2 \sin\theta \end{Bmatrix} \quad (2)$$

The steady lateral forces, represented by  $F_x$  and  $F_y$ , can be considered as the sum of two forces: a fixed force, represented by  $F_{ox}$  and  $F_{oy}$ , which the impeller would experience if located at the volute center, and a force due to the eccentric

displacement of the impeller, represented by a "stiffness" matrix  $[A]$ . By taking data at four fixed eccentric positions of the impeller, 90 degrees apart, the matrix  $[A]$  and the vector  $\{F_o\}$  can be extracted. The gravitational and buoyancy forces on the rotor are subtracted out.

## EXPERIMENTS

In references 6-8 results were presented for a typical impeller (impeller X), a five bladed Byron-Jackson centrifugal impeller with a specific speed of 0.57, operating in a spiral volute (volute A) at various impeller speeds ( $\leq 2000$  rpm) and flow rates. In order to test under cavitating conditions, the impeller speed was increased to 3000 rpm and the water was substantially de-aerated.

In the following pages the results for three different flow rates are presented: the flow rates chosen are below design ( $\phi=0.060$ ), design ( $\phi=0.092$ ) and above design ( $\phi=0.104$ ). Cavitation performance curves for each of these flow rates are presented in figure 2. We observe that the breakdown cavitation numbers for the three flow rates tested are 0.17, 0.26 and 0.30 respectively.

## RESULTS

Results for the radial forces,  $F_{ox}$  and  $F_{oy}$ , and for the stiffness coefficients are presented in figures 3 through 8. A quick glance will show that large changes occur in both characteristics as the pump approaches and passes through breakdown. Notice that the steady force shown in figures 3 and 4 changes in both magnitude and direction.

Figures 3 and 4 show that for  $\phi=0.060$  the magnitude of  $\{F_o\}$  decreases with performance loss with a small change in direction. For both  $\phi=0.092$  and  $\phi=0.104$ , the magnitude of  $\{F_o\}$  has a minimum with decreasing head coefficient. For each flow coefficient, the direction of  $\{F_o\}$  rotates away from the tongue. For  $\phi=0.092$ ,  $\{F_o\}$  rotates through more than  $180^\circ$  as the pump progresses through breakdown.

Figures 5-8 show the hydrodynamic force matrix  $[A]$  from equation (2). These no-whirl results correspond to  $-[K]$  of the quadratic fit of reference 2 to whirl data for mass, damping and stiffness matrices. The three flow coefficients exhibit the same trends. The diagonal elements decrease with performance loss. The off-diagonal elements first decrease slightly in magnitude with lower cavitation number then increase with performance loss. Figure 8 indicates that the off-diagonal elements do not change monotonically with head coefficient.

In summary, cavitation affects the steady forces, both the impeller-centered force  $\{F_o\}$  and the hydrodynamic force matrix  $[A]$ , exerted upon an eccentric impeller. It is useful to interpret the matrix  $[A]$  in terms of the average normal force,  $F_N$ , and the tangential force,  $F_T$ , acting on a whirling impeller in the limit as the whirl speed approaches zero. With cavitation breakdown, the normal force is reduced while the tangential force is increased. Further tests are planned to examine the unsteady flow effects which occur at non-zero whirl speed. More specifically, the frequency dependence in the matrix  $[A]$  (the damping and added mass components) will shortly be examined as a function of cavitation number.

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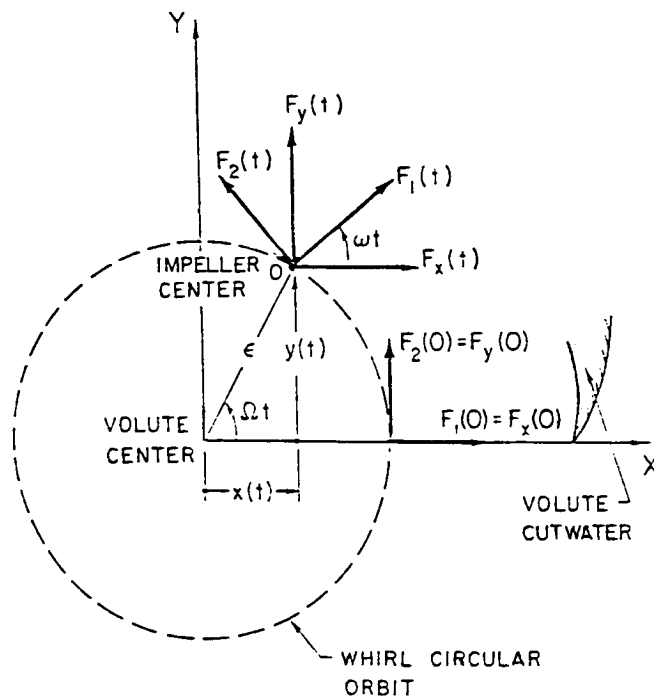


Figure 1 Schematic representation of the position of the impeller within the volute. The measured forces are indicated in the rotating dynamometer frame (as  $F_1$ ,  $F_2$ ) and in the stationary volute frame (as  $F_x$ ,  $F_y$ ).

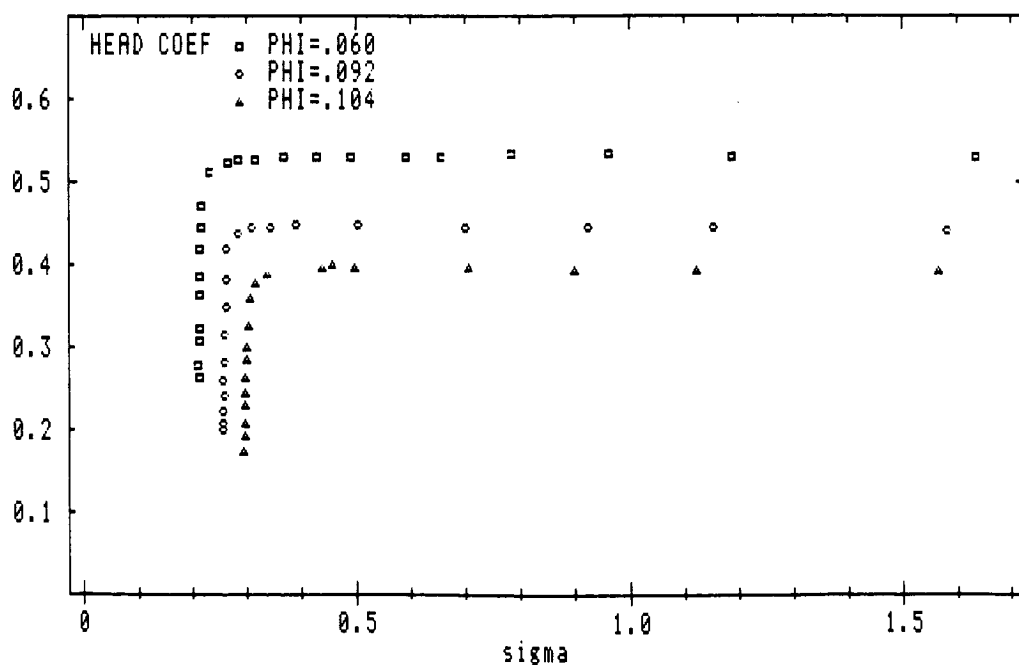


Figure 2 Cavitation performance curves for the three flow coefficients:  $\phi=0.060$  (below design),  $\phi=0.092$  (design) and  $\phi=0.104$  (above design), for volute A/impeller X at 3000 rpm.

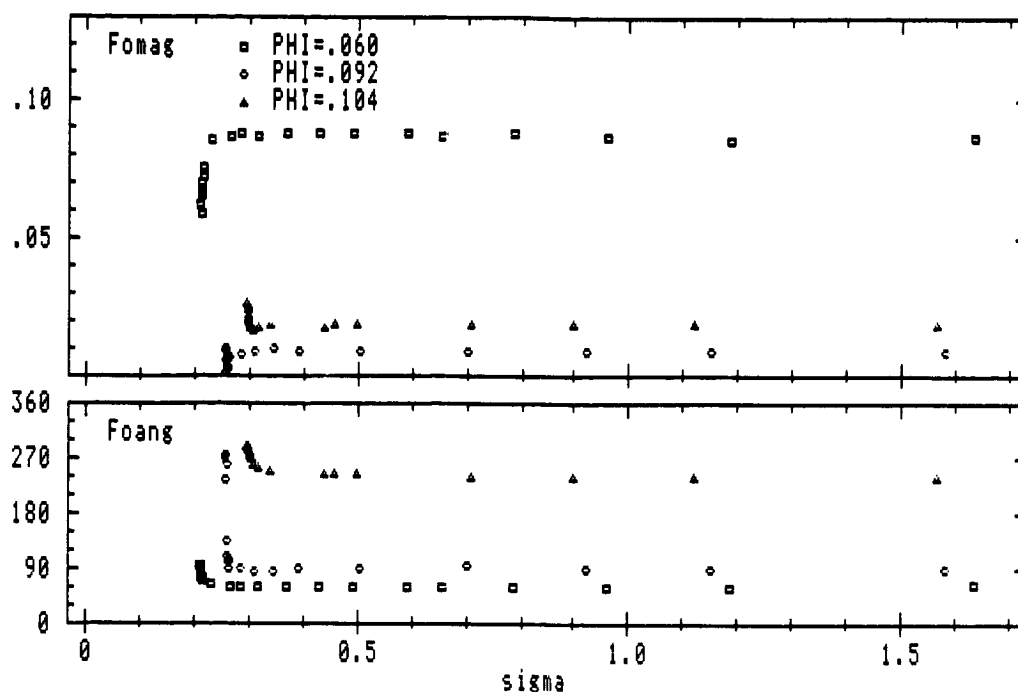


Figure 3 The dependence of the magnitude and direction of the volute force,  $\{F\}$ , on cavitation number for the three flow coefficients:  $\phi=0.060$ ,  $\phi=0.092$ ,  $\phi=0.104$ , for volute A/impeller X at 3000 rpm.

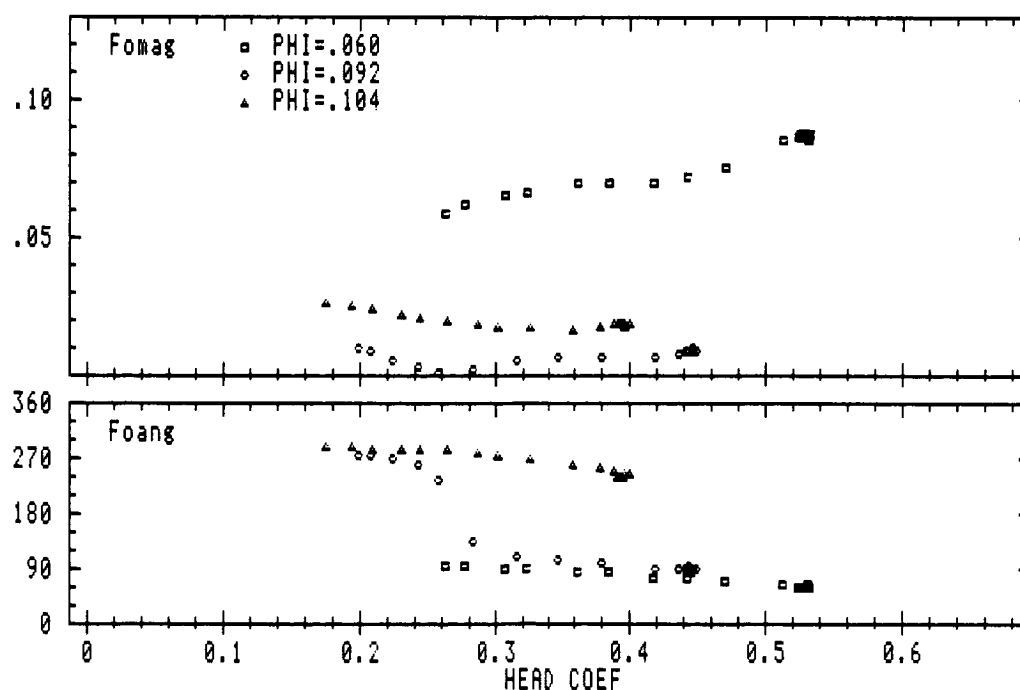


Figure 4 The dependence of the magnitude and direction of the volute force,  $\{F\}$ , on head coefficient for the three flow coefficients:  $\phi=0.060$ ,  $\phi=0.092$ ,  $\phi=0.104$ , for volute A/impeller X at 3000 rpm.

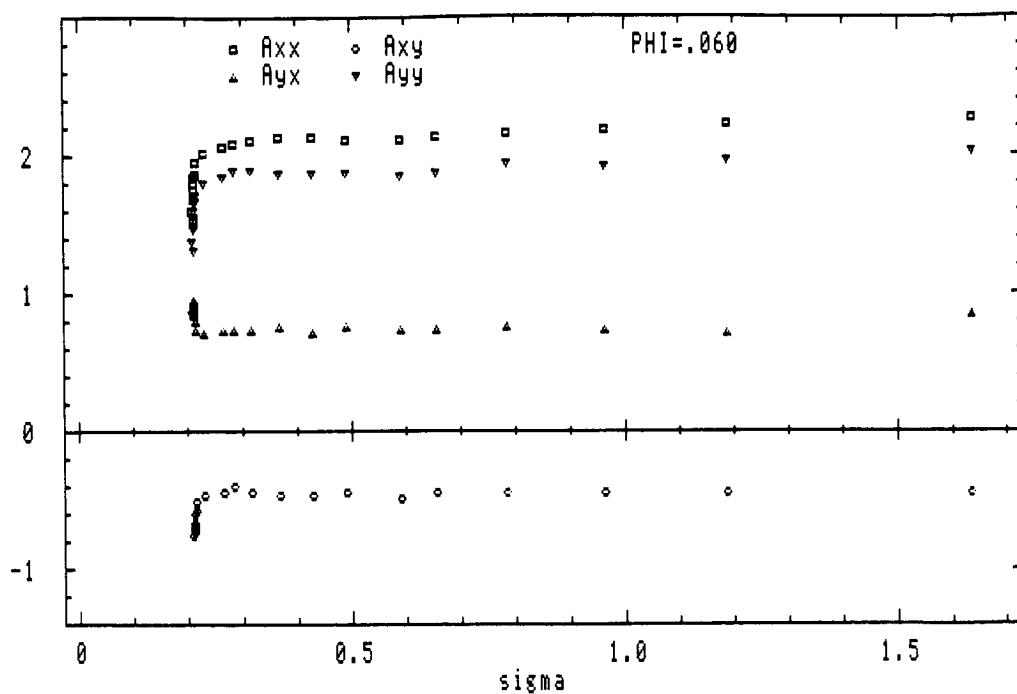


Figure 5 The dependence of the elements of the hydrodynamic force matrix,  $[A]$ , on cavitation number for  $\phi=0.060$  (below design), for volute A/impeller X at 3000 rpm.

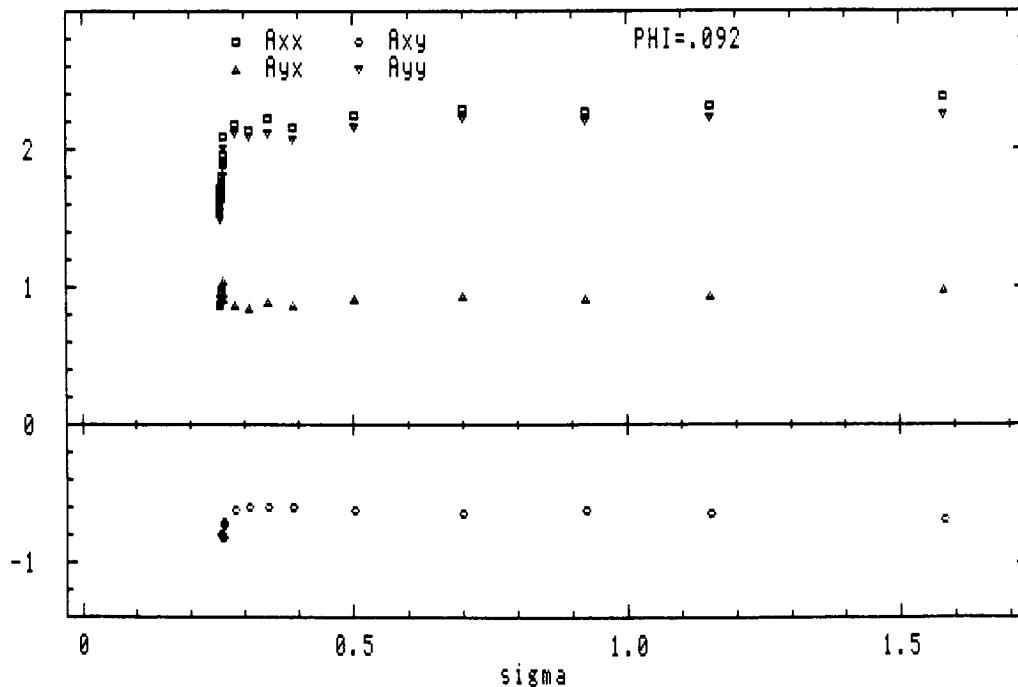


Figure 6 The dependence of the elements of the hydrodynamic force matrix,  $[A]$ , on cavitation number for  $\phi=0.092$  (at design), for volute A/impeller X at 3000 rpm.



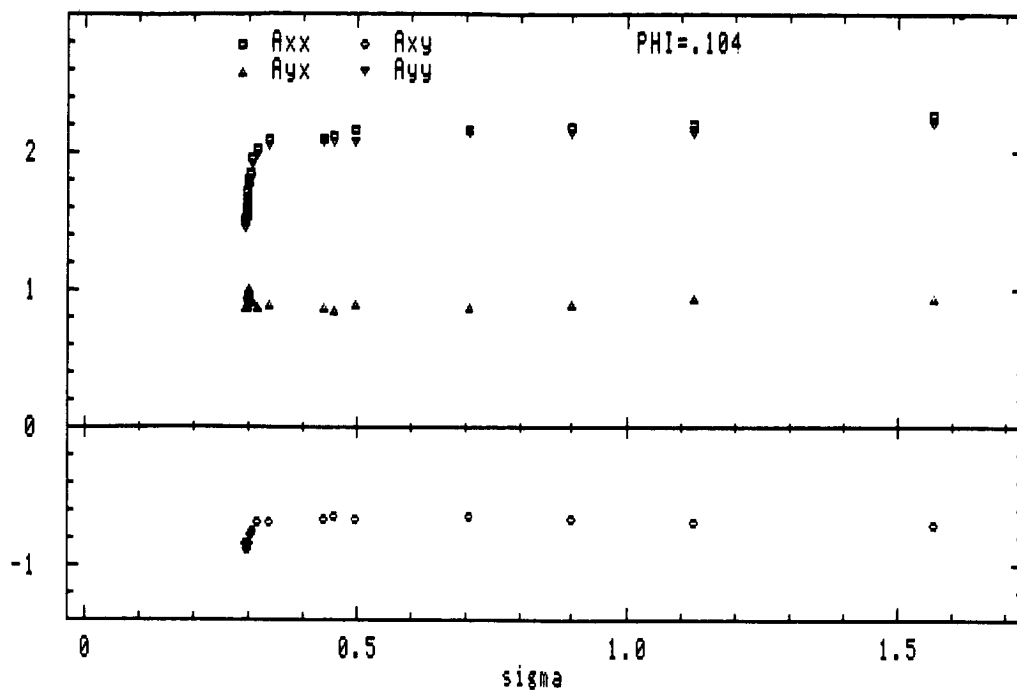


Figure 7 The dependence of the elements of the hydrodynamic force matrix,  $[A]$ , on cavitation number for  $\phi=0.104$  (above design), for volute A/impeller X at 3000 rpm.

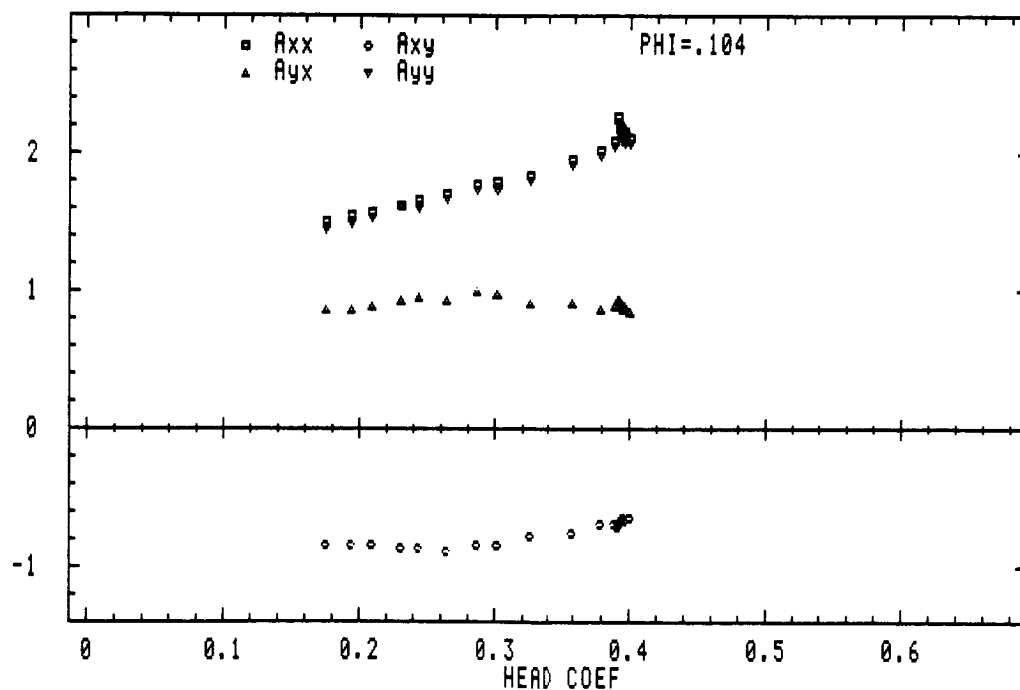


Figure 8 The dependence of the elements of the hydrodynamic force matrix,  $[A]$ , on head coefficient for  $\phi=0.104$  (above design), for volute A/impeller X at 3000 rpm.